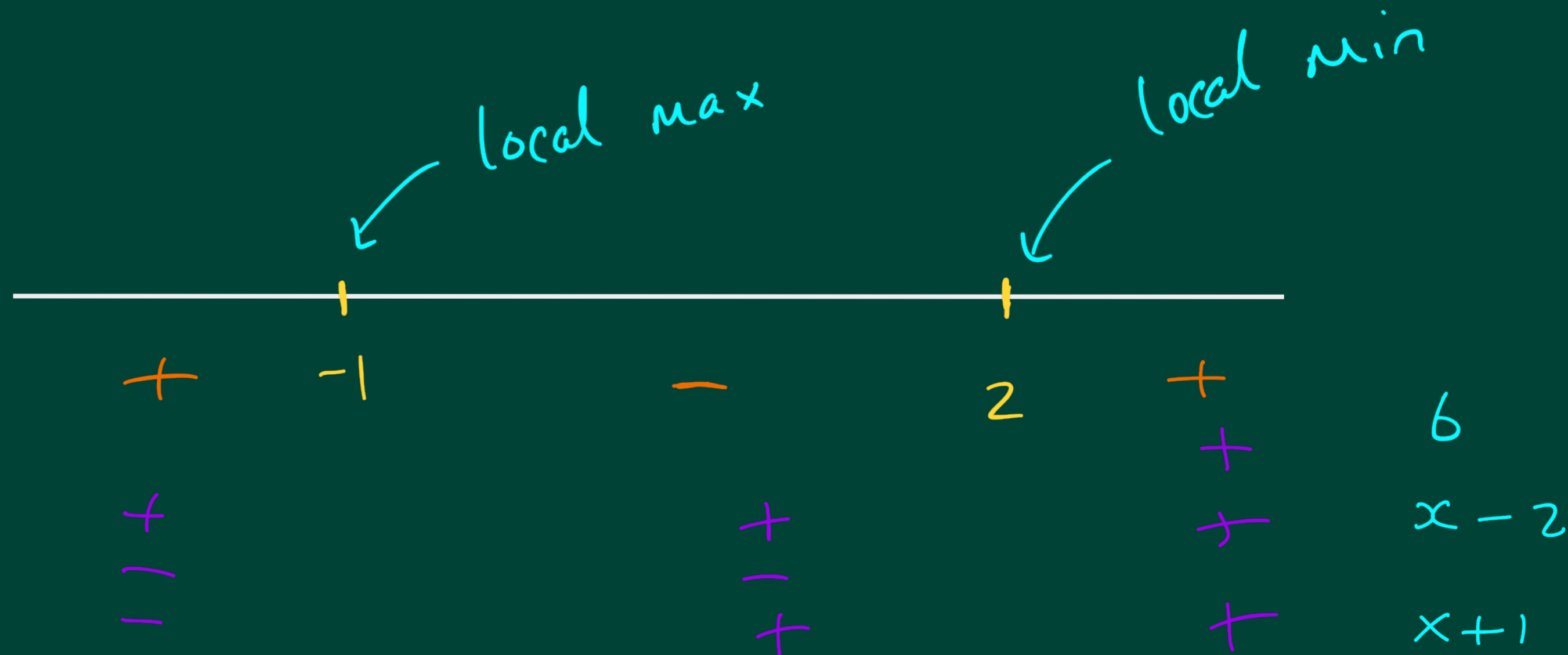


$$f'(x) = 6x^2 - 6x - 12 = 6(x^2 - x - 2)$$

$$= 6(x - 2)(x + 1)$$

$$f'(x) = 0 \quad @ \quad 2 \quad \text{and} \quad -1$$

$$f'(x) = 6(x - 2)(x + 1)$$



$$f(x) = x^{1/3} (x^2 - 4)$$

$$f'(x) = \frac{1}{3} x^{-2/3} (x^2 - 4) + x^{1/3} (2x)$$

$$= \frac{x^2 - 4}{3x^{2/3}} + x^{1/3} (2x)$$

Critical pt @ $x=0$ as $f'(0)$ is undefined.

Say $\frac{x^2 - 4}{3x^{2/3}} + x^{1/3} (2x) = 0, x \neq 0$

$$x^2 - 4 + 3x^{2/3} x^{1/3} 2x = 0$$

$$x^2 - 4 + 6x^2 = 0$$

$$7x^2 - 4 = 0$$

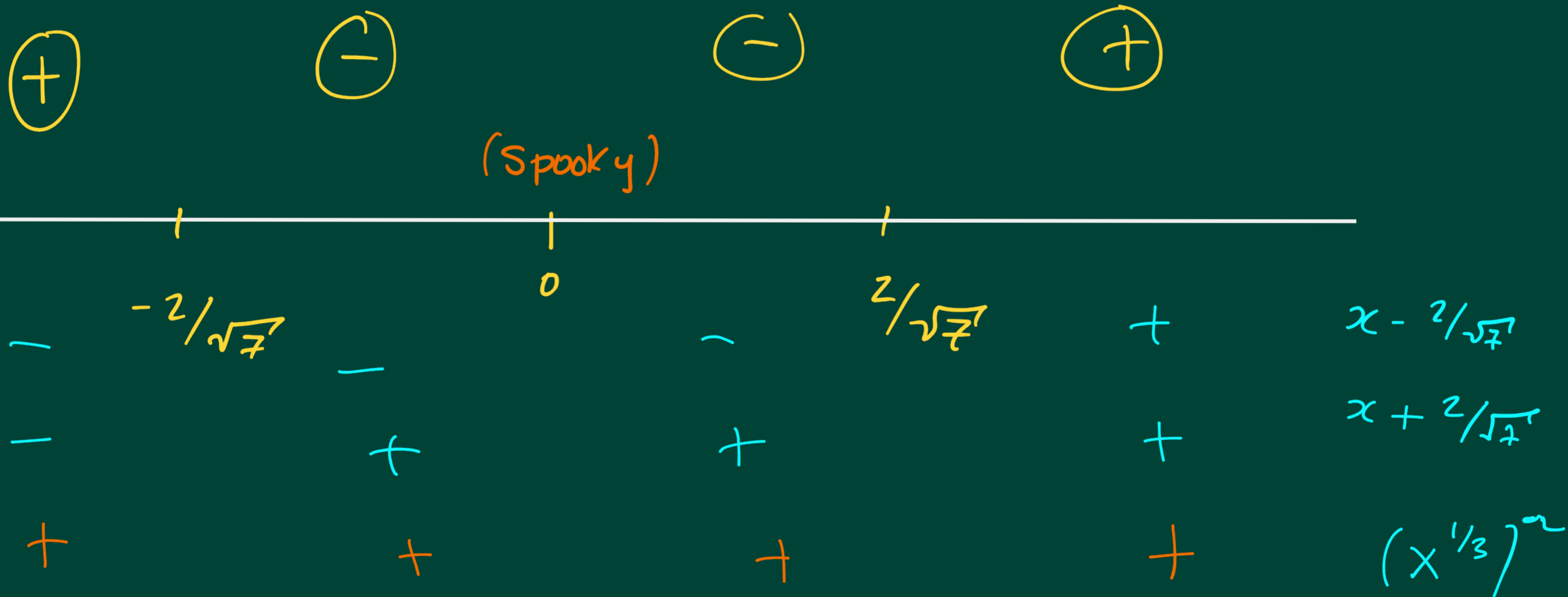
$$7x^2 = 4$$

$$x^2 = 4/7$$

$$x = \pm 2/\sqrt{7}$$

$$f'(x) = \frac{7x^2 - 4}{3x^{2/3}} = \frac{7\left(x - \frac{2}{\sqrt{7}}\right)\left(x + \frac{2}{\sqrt{7}}\right)}{3x^{2/3}}$$

$$f'(x) = \frac{7x^2 - 4}{3x^{2/3}} = \frac{7\left(x - \frac{2}{\sqrt{7}}\right)\left(x + \frac{2}{\sqrt{7}}\right)}{3x^{2/3}}$$



② $-\frac{2}{\sqrt{7}}$ we have a local max

③ $\frac{2}{\sqrt{7}}$ we have a local min

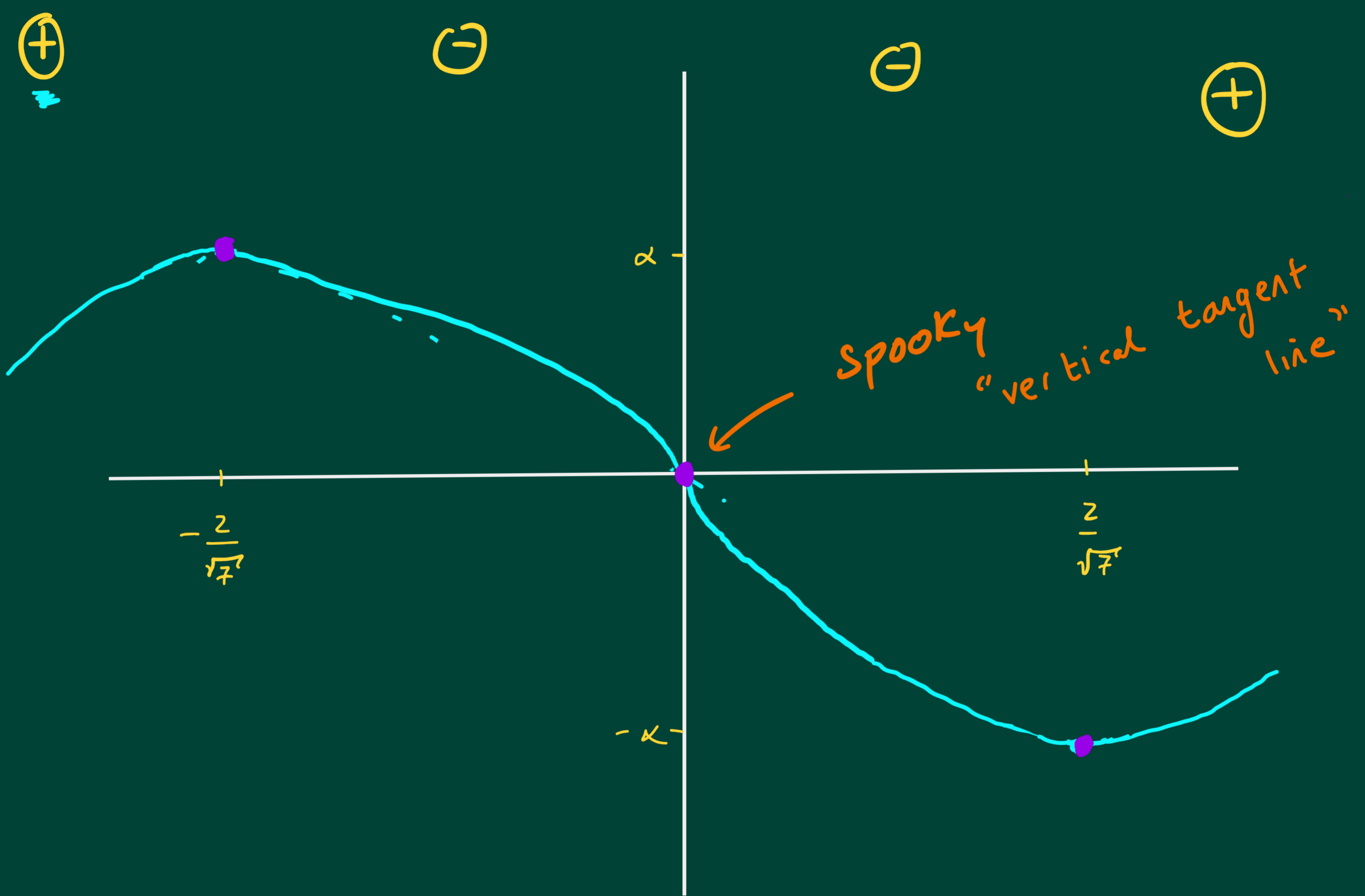
④ 0 we have $f'(0)$ undefined.

$$f(x) = x^{1/3} (x^2 - 4)$$

$$\begin{aligned} f\left(-\frac{2}{\sqrt{7}}\right) &= \left(-\frac{2}{\sqrt{7}}\right)^{1/3} \left(\left(-\frac{2}{\sqrt{7}}\right)^2 - 4\right) \\ &= \left(-\frac{2}{\sqrt{7}}\right)^{1/3} \left(-\frac{24}{7}\right) > 0 \end{aligned}$$

$$\begin{aligned} f\left(\frac{2}{\sqrt{7}}\right) &= \left(\frac{2}{\sqrt{7}}\right)^{1/3} \left(\left(\frac{2}{\sqrt{7}}\right)^2 - 4\right) \\ &= \underbrace{\left(\frac{2}{\sqrt{7}}\right)^{1/3} \left(-\frac{24}{7}\right)}_{-\alpha} < 0 \end{aligned}$$

$$f(0) = 0$$



$(+)$

$(-)$

$(-)$

$(+)$

α

SPOOKY
"vertical tangent line"

$-\frac{2}{\sqrt{7}}$

$\frac{2}{\sqrt{7}}$

$-\alpha$